Application of Improved Crow Search Algorithm in MPPT of Photovoltaic Arrays under Partial Shading Conditions

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Abstract: Under the condition of partial shading, the Power-Voltage curve of photovoltaic array presents a characteristic of multi-peak, when conventional maximum power point tracking (MPPT) algorithms, like Perturb and Observe method (PO), fail to track efficiently. Crow search algorithm (CSA) has outstanding global search capability, because of which it is used to track maximum power point under the condition of partial shading. But it also has the problems in local optimum and oscillating amplitude. To solve those problems, both of an auto judgment of power output and an optimization-orientation guided by elite individuals are introduced. The results presented in MATLAB/Simulink that the application of improved CSA in MPPT can track efficiently with lower level of oscillating amplitude.

Keywords: PV system, PO Method, MPPT, CSA, Elite individual

1. Introduction

To solve the deteriorating global environment and insufficient energy reserves, renewable energy sources such as solar power are gaining prominence as primary alternatives [1-2]. A photovoltaic (PV) array can output its maximum power under special temperature and solar irradiance conditions at a particular voltage. By using the impedance matching principle in the equivalent model of the PV array, this voltage point can be calculated and tracked. The process of tracking this maximum power point (MPP) using power electronic technologies [3] is referred to as maximum power point tracking (MPPT).

Traditional MPPT algorithms include three main methods: the Perturb and Observe method (PO), the Incremental Conductance method (INC), and the Constant Voltage method (CV). At the beginning, literatures [4-7] compared the output characteristics of these above-mentioned methods and proposed an improved PO algorithm aimed at the false trips in the PO method. However, in scenes such as partial shading of PV panels, traditional algorithms often fail to track effectively. Consequently, replacing traditional MPPT algorithms with intelligent algorithms has become a research trend. To solve the multi-peak output problem caused by partial shading, literatures [8-11] proposed the Particle Swarm Optimization (PSO) algorithm. This algorithm effectively resolves the challenges of multi-peak output tracking and local optimum under partial shading conditions. However, it still faces issues such as parameter adaptability. Literatures [12-15] introduced the Fuzzy Logic Control method, but this method heavily depends on the designer's expertise and intuition. Moreover, insufficient training data can lead to poor model performance. In summary, current MPPT

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research faces the following challenges:1) Limited robustness of MPPT algorithms.2) Significant power output oscillation amplitudes.

To solve these challenges, this paper proposes an MPPT control algorithm based on an improved Crow Search Algorithm (CSA). Using a PV array integrated with a boost circuit topology under partial shading conditions, this study conducts simulations in MATLAB/Simulink. The proposed method is compared with the traditional PO method under varying solar irradiance and temperature conditions in partial shading scenes. The proposed approach offers the following innovations:

1) The traditional CSA algorithm is enhanced with an auto judgment of power output to avoid local optimum.

2) Based on the first improvement, an enhanced CSA algorithm incorporating elite individuals replaces the traditional CSA algorithm, effectively reducing the amplitude of power output oscillations.

The structure of this paper is as follows: Section II represents the modeling of the PV system and introduction of the integrated circuit. The principles of traditional PO tracking, the traditional CSA algorithm, and the improved CSA algorithm are revealed in Section II. Section IV shows simulation in MATLAB/Simulink and analysis.

2. System Modeling and Circuit Integration

2.1. Photovoltaic System Modeling

Solar cells are the fundamental components of solar photovoltaic systems. Their I-U and P-U characteristics are influenced by solar irradiance, ambient temperature, and the parameters of the PN junction in the solar cells, exhibiting a nonlinear relationship [16]. Based on these characteristics, an equivalent circuit model of solar cells can be established. Commonly used equivalent circuit models include the single-diode model and the dual-diode model. The single-diode model is widely used because it accurately reflects the working principles of solar cells with a simple circuit topology. The circuit diagram of the single-diode model is shown in Figure 1.



Figure 1: Single diode equivalent model of solar cell

where the photocurrent I_{ph} generated by the solar cell is represented as a current source with an equivalent current value. The PN junction in the solar cell is represented by a parallel diode, while losses due to the material properties of the solar cell are represented by a series resistance R_s and a paralleled one R_{sh} . According to Kirchhoff's current law, the following equation can be derived from the circuit in Figure 1:

$$I = I_{ph} - I_d - I_{sh}$$
(1-1).

The characteristic equation of the solar cell can be obtained as Equation(1-2)[17]:

$$I = I_{ph} - I_0 \cdot (e^{(q \cdot (U + I \cdot R_s)/(A \cdot K \cdot T))} - 1) - \frac{I \cdot R_s + U}{R_{sh}}$$
(1-2),

where I_0 is the reverse saturation current of the diode, q is the elementary charge, R_s is the series resistance, A is the ideality factor of the PN junction, K is Boltzmann's constant, and T is the absolute temperature in Kelvin.

Since Equation (1-2) is transcendental and complex to solve, it needs to be properly simplified. The order of magnitude of R_{sh} is typically 10³ times larger than R_s , allowing $\frac{I \cdot R_s + U}{R_{sh}}$ to be ignored. The forward current of the diode is approximately zero due to manufacturing processes, making I_{ph} approximately equal to the short-circuit current I_{sc} of the circuit shown in Figure 1. Hence, Equation (1-2) can be simplified as:

$$= I_{sc} \cdot [1 - C_1 \cdot (e^{\frac{V}{C_2 \cdot V_{oc}}} - 1)]$$
(1-3),

where V_{oc} is the open-circuit voltage, $C_1 = \frac{I_0}{I_{sc}}$, $C_2 = \frac{AKT}{Q}$.

At MPP, substituting the voltage V_m and current I_m into Equation (1-3) yields:

$$I_m = I_{sc} \cdot [1 - C_1 \cdot (e^{\frac{V_m}{C_2 \cdot V_{oc}}} - 1)]$$
(1-4),

Assuming $e^{\frac{V}{C_2 \cdot V_{oc}}} \gg 1$, Equation (1-4) can be further simplified to:

$$C_1 = \left(1 - \frac{l_m}{l_{sc}}\right) \cdot e^{\frac{V_m}{C_2 \cdot V_{oc}}}$$
(1-5),

By substituting the open-circuit state I = 0, $U = V_{oc}$, Equation (1-5) becomes:

$$= I_{sc} \cdot \left[1 - (1 - \frac{I_m}{I_{sc}}) \cdot e^{\frac{-V_m}{C_2 \cdot V_{oc}}} \cdot (e^{\frac{1}{C_2}} - 1)\right]$$
(1-6),

Assuming $e^{\frac{1}{c_2}} \gg 1$, the equation is further simplified to:

$$C_2 = \left(\frac{V_m}{V_{oc}} - I\right) \left[\ln(1 - \frac{I_m}{I_{sc}})\right]^{-1} (1-7).$$

Solar cell manufacturers typically provide the maximum power point voltage V_{m_ref} and current I_{m_ref} measured under standard test conditions (STC), i.e., standard temperature ($T_{ref} = 25^{\circ}C$) and standard irradiance ($S_{ref} = 1000W/m^2$). Variations in temperature and solar irradiance affect photon generation in solar cells, necessitating corrections to I_m , I_{sc} , V_m , V_{oc} using Equations (1-8) to (1-13):

$$\Delta T = T - T_{ref} \tag{1-8},$$

$$\Delta S = \frac{S}{S_{ref}} - 1 \tag{1-9},$$

$$I_{sc} = I_{sc_ref} \cdot \frac{s}{s_{ref}} \cdot (1 + \alpha \Delta T)$$
(1-10),

$$V_{oc} = V_{oc_ref} \cdot (1 - \gamma \Delta T) \cdot \ln(e + \beta \Delta S)$$
(1-11),

$$I_m = I_{m_ref} \cdot \frac{s}{s_{ref}} \cdot (1 + \alpha \Delta T)$$
(1-12),

$$V_m = V_{m_ref} \cdot (1 - \gamma \Delta T) \cdot \ln(e + \beta \Delta S)$$
(1-13),

where α , β , γ are all constants, commonly taking values as $\alpha = 0.0025$, $\beta = 0.5$, $\gamma = 0.00288$.

2.2. Output Characteristics of PV Systems under Partial Shading [24]

Using two identical PV modules connected in series as an example, the single-diode equivalent model established above is used for analysis. Under partial shading, various levels of irradiance on the PV modules result in varying short-circuit currents I_{sc} . When the output current of the PV array lies between the short-circuit currents of the two modules, the diode in the module with the lower I_{sc} conducts, and the output characteristic is determined by the module with the higher I_{sc} . When the output current is insufficient to activate the diode of the module with the lower I_{sc} , the output characteristic of the PV array equals the combined output characteristics of both modules.

When the PV array consists of multiple series-connected modules, the analysis process remains the same. This paper studies a PV array consisting of three identical modules in series. The parameters for each module are as follows:

Parameter	Value	Unit
Open-circuit voltage Voc	21.7	V
Voltage at MPP V_m	15	V
Short-circuit current Isc	4.8	Α
Current at MPP I_m	3.7	Α
Maximum power P_m	55.5	W

Table 1: Essential parameters of PV module

2.3. Boost Converter Circuit [18]



Figure 2: Boost circuit boarded with MPPT module.

where C_1 is the filtering capacitor that stabilizes the output voltage. The IGBT switch Q_1 , controlled appropriately, works with the diode D_1 to allow the inductor L_1 to absorb and release energy. When Q_1 conducts, current flows through L, storing energy from the input voltage, while the load is powered by C_1 . When Q_1 is off, L releases the stored energy, powering the load with energy from both C_1 and L. A sufficiently large inductor ensures continuous current operation in the boost circuit. By adjusting the duty cycle of Q_1 , the output voltage can be controlled to exceed the input voltage, achieving voltage boosting.

3. MPPT Algorithms

3.1. PO Method [4]

The principle of the PO method is as follows: a small perturbation is applied to the PV system, and the change in output power before and after the perturbation is observed. If the output power increases, it indicates that the current voltage is less than V_{mpp} , and the output voltage needs to be increased; otherwise, the output voltage should be decreased. To avoid misjudgment, the difference in power dP and the difference in voltage dV before and after the perturbation $\left(\frac{dP}{dV}\right)$ are introduced for evaluation.

The relationship between the signs of dP, dV, and whether the output voltage should be increased is discussed as following false code:

Algorithm 1: the PO voltage adjustment		
1. if $dP < 0$ then		
2.	$\inf_{d} dV < 0 \text{ then}$	
3.	Output: "Increase Output Voltage"	
4.	else if $dV > 0$ then	
5.	Output: "Decrease Output Voltage"	
6. else if $dP > 0$ then		
7.	if $dV > 0$ then	
8.	Output: "Increase Output Voltage"	
9.	9. else if $dV < 0$ then	
10.	Output: "Decrease Output Voltage"	
11. End		

3.2. CSA

CSA is an intelligent optimization algorithm proposed in 2016 by Askarzadeh et al., inspired by the natural foraging behavior of crows. Crows have the habit of storing excess food and, to obtain more food, they follow other crows that have found food, discovered their storage locations, and steal the food. If a crow detects that it is being followed, it will randomly fly to confuse its pursuers.

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Figure 3: The compared processes of CSA(a) and Improved CSA(IMCSA)(b)

The parameters that need to be initialized include the size of the crow population N, the maximum number of iterations, the flight length fl, and the awareness probability AP. The fitness function f(x) should be designed according to specific requirements, and its value evaluates the quality of a crow's position: the higher the fitness function value, the better the crow's current position; conversely, a lower value indicates a worse position.

Subsequently, the algorithm randomly generates the initial positions $x_i(t)$ of the crows and their memory of the best positions $m_i(t)$, representing the locations of stored food. During the iterative process of the algorithm, an individual crow randomly selects another crow as its tracking target, with the probability of being discovered set to *AP*. If crow *a* is discovered by crow *b* during tracking, *a* will randomly choose a new flight destination. Otherwise, *a* will attempt to approach *b*'s stored food location. This process can be expressed by Equation (3-1).

$$x_{i} = \begin{cases} x_{i} + r_{1} \cdot fl \cdot (m_{i}(t) - x_{i}(t)) & r_{2} \ge AP \\ random & otherwise \end{cases}$$
(3-1)

At the end of each iteration, the positions of the crows are re-evaluated using the fitness function. These are then compared with the best positions stored in their memory. If the current position is better than the memorized best position, the crow's memory is updated accordingly. This process can be expressed by Equation (3-2).

$$m_{i}(t+1) = \begin{cases} x_{i}(t+1) \ f(x_{i}(t+1)) < f(m_{i}(t)) \\ m_{i}(t) & otherwise \end{cases}$$
(3-2)

Until the iteration times reached its upper limit, the algorithm outputs its result.

3.3. Optimization-Oriented Crow Search Algorithm Guided by Elite Individuals

Based on the above characteristics, reference [20] proposes an optimization strategy that establishes elite individuals according to the amount of stored food and uses their memorized positions as guidance. In this strategy, the top *s* crows with the highest stored food quantities are designated as elite individuals, while the remaining N - s crows are classified as ordinary individuals. At time *t*, the amount of food stored by crow *k* is represented by the fitness value of its storage location.

To prevent their food from being stolen, elite individuals usually operate near their nests and do not attempt to steal from others. Based on this behavior, the position of elite individuals can be determined using Equation (3-3).

$$x_{i,j}(t+1) = \begin{cases} m_{i,j}(t) + (2r_1 - 1) \times (m_{i,j}(t) - 1) & r_2 \\ m_{i,j}(t) + (2r_1 - 1) \times m_{i,j}(t) & otherwise \end{cases}$$
(3-3)

where j = 1, 2, ..., D, while D represents the dimensionality of the search space, and r_1, r_2 are random numbers within the interval [0,1].

The behavior of ordinary individuals remains consistent with that of crows prior to the improvement. Their positions can be determined using the improved version of Equation (3-2), which is represented as Equation (3-4).

$$x_{i,j}(t+1) = \begin{cases} x_{i,j}(t) + r_1 \cdot fl(t) \cdot (m_{k,j}(t) - x_{i,j}(t)) & r_2 > AP \\ random & otherwise \end{cases}$$
(3-4)

where $m_k(t) = [m_{k,1}(t)...m_{k,D}(t)]$ represents the food storage nest of elite individual k, and individual k is randomly selected from the elite individuals. r_1, r_2 are random numbers within the interval [0,1]. $fl(t) = 0.5 \cdot \exp(1 - \frac{t}{T})^2$ is the flight step size function of crow *i*. *t* is the search time variable. *T* is the upper limit of the search time.

3.4. Application of the Improved Crow Search Algorithm in MPPT

The improved CSA is applied to PV MPPT. In the algorithm, each crow individual represents the output voltage of the current photovoltaic system, with each individual tasked with finding the maximum power point voltage V_m . The final output result will be the maximum power point voltage V_m . The crow's flight step size corresponds to the voltage increment generated during each iteration of the MPPT process. The dimensionality of the search space corresponds to the number of variables that need to be optimized by the algorithm. In this study, since the output voltage and output current of the PV system need to be optimized, the dimensionality is set to 2. To ensure that the voltage and current stay within a limited range, a condition is introduced: if the output power corresponding to a particular individual's voltage exceeds 100W, the position of that individual is no longer updated. Additionally, 30 new individuals are generated at the last maximum power point of that individual. These new individuals update their velocity according to the two-dimensional particle swarm velocity formula (Equation 3-5). Here, v represents the velocity of the individual, w is the inertia weight, c is the learning factor, *best* is the individual's best position, and r_3 is a random number used to expand the search space. This modified algorithm will be referred to as the IMCSA algorithm.

 $v = w \cdot v + c \cdot r_3(u_array(best) - x)$ (Equation 3-5).

The steps of applying IMCSA to MPPT are as follows:

Step 1: Initialize the parameters and design the fitness function f(x) with boundaries.

Step 2: Generate the initial positions of *N* crow individuals randomly within the two-dimensional search space using random numbers from the interval [0,1].

Step 3: Calculate the fitness values according to f(x) for each initial position and select the top s crows with the highest fitness values as elite individuals.

Step 4: Begin tracking the photovoltaic system's maximum power point. Elite individuals update their positions according to Equation (3-3), while ordinary individuals update their positions according to Equation (3-4).

Step 5: Update the memory of the crow individuals, i.e., the food storage positions, based on Equation (2-2).

Step 6: Check if the maximum number of iterations has been reached. If yes, terminate the iteration and output the result. If no, return to Step 4.

4. Simulation and Analysis

A model for photovoltaic array MPPT control was established in MATLAB/Simulink [21]. The simulation time is set to 6 seconds, with a system sampling period of 1e-05 seconds. The solver algorithm is automatically selected from variable step-size algorithms. The simulation circuit diagram is shown in Figure 5, and the parameters of the circuit components are listed in Table 3.

Component	Value	Unit
C_1	470e-6	F
C_2	47e-6	F
R_1	50	Ω
L_1	1.2e-3	L

Table 3: Parameters of the simulation circuit components

Three series-connected photovoltaic modules were used, with solar irradiance values of 1000 W/m², 800 W/m², and 600 W/m² applied to simulate partial shading conditions. The temperature of all three photovoltaic modules was maintained at 25°C. Under these partial shading conditions, 50 simulation experiments were conducted for the PO, CSA MPPT, and IMCSA MPPT algorithms. In each experiment, the initial duty cycle of the three methods was set to 0.5. For both the CSA and IMCSA algorithms, the number of crow individuals (particles) was 50, and the maximum number of iterations was 30.



Figure 4: The current-voltage curve of PV _ array

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Figure 5: The power-voltage curve of PV array



Figure 6: Overall comparison of output power for PO, CSA, and IMCSA algorithms and local comparison between CSA and IMCSA algorithms

Figure 6 shows the simulation results of the PO, CSA, and IMCSA algorithms. The results are presented sequentially from left to right and top to bottom, displaying output power, duty cycle, output voltage, and output current. From the results, it can be observed that under this partial shading condition: The PO algorithm stabilizes the output power waveform of the photovoltaic array at 0.45s, the CSA algorithm stabilizes at 0.19s, and the IMCSA algorithm stabilizes at 0.22s.

In terms of output power: The output power value of the PO algorithm is 103,431W the CSA is 120.753W, and the IMCSA is 120.791W.

Thus, the CSA and IMCSA algorithms significantly outperform the PO algorithm in this aspect, with an improvement of 16.46% and 16.78%.

In terms of output power oscillation amplitude: The oscillation amplitude of the PO algorithm is 0.744W, the oscillation amplitude of the CSA algorithm is 0.293W, and the oscillation amplitude of the IMCSA algorithm is 0.250W.

The IMCSA algorithm achieves reductions in oscillation amplitude of 17.20% compared to the CSA algorithm and 153.92% compared to the PO algorithm.

In summary^[23], the proposed IMCSA algorithm achieves optimal fitness values, with the smallest oscillation amplitude and minimal power tracking loss. This enhances the stability and accuracy of MPPT, optimizing photovoltaic power generation efficiency.

5. Conclusion

Under variable solar irradiance conditions, photovoltaic cell output P-U curves exhibit large oscillation amplitudes and other issues. Traditional MPPT algorithms have slow tracking speeds and low tracking accuracy. This paper proposes an improved crow search algorithm (CSA), which leverages the guiding effect of elite individuals to enhance the motion strategy of crow populations. The output voltage, current, and power of the traditional PO, CSA, and the improved ADCSA algorithms were compared.

Simulation results demonstrate that under variable solar irradiance conditions, the improved ADCSA algorithm achieves faster maximum power point tracking with smaller oscillation amplitudes compared to the other two algorithms. This highlights the robustness of the proposed algorithm in adapting to environmental changes. Thus, the improved ADCSA algorithm is more adaptive, responsive, accurate, and stable under varying solar irradiance conditions, significantly improving power generation efficiency.

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