

A multivariate LSTM-based deep learning model for stock market prediction

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Abstract. Stocks represent ownership in a company and a proportionate claim on its assets and earnings. Investors trade stocks via an exchange by buying at a price and selling at a higher price. Due to market volatility forecast it is a necessity for trading to determine the direction of the stock price in order to maximize profit and minimize loss. Traditional methods of stock price predictions include technical and fundamental analysis. The technical deals with historical price movement while fundamental analysis uses the relationship between financial information about the company. However, these predictions methods sometimes fail to yield desired result sometimes due to the influence of factors such as national policies, global and regional economics, psychological, human among many. This work proposes a prediction model for stock market using LSTM algorithm. Multivariate time series stock price data is obtained from Nigerian Stock Exchange Index to implement the model. The experimental result of the technique is measured using MAPE, MAE, MSE and rRMSE performance metrics. The accuracy of the result shows that the proposed system outperforms existing traditional and deep learning methods.

Keywords: deep learning, multivariate, stock price prediction, long short-term memory.

1. Introduction

Stock is a share of the assets of an organization which have some value or price associated with it. The place where stocks are made available to the public is known as stock market. Investors usually trade on the market by buying and selling stocks with the aim of making profit when the price goes higher than it was purchased [1].

Predicting the direction of price movement with some accuracy is necessary to determine buying and selling stock. Investors focus on stock price prediction in order to yield significant profits. Traditional stock price prediction methods include technical analysis, fundamental analysis and time series. The technical analysis use historical price movement to predict price pattern while the fundamental analysis use the financial information about the company such as inventory or revenue growth relates [2]. Time series method involves using historical performance for prediction with current observations dependent on past observation in time [3]. However, it sometimes fails to accurately forecast the financial market because of national and global economic trends [4].

Deep learning (DL) models are recent methods that have also successfully analyzed time series data more accurately when compared to the other traditional methods [5], [6]. The DL models is able to learn complex mappings of multiple inputs and outputs. The work aims to develop a model based on LSTM and multivariate time series to predict stock price. The work is introduced in Section 1. Section 2 presents

some related works. The methodology for the proposed model is discussed in section 3. The experiments and analysis of the model is discussed in section 4. Finally, the work is concluded in in Section 5.

2. Literature review

A review of existing research work on stock prediction using machine learning techniques is discussed. Gozalpour and Teshnehlab [7] proposed the closing price prediction model using Jordan Recursive Neural Network (JRNN) model. Data used on the model include Microsoft Corporation, NAS-DAQ symbols, Intel Corporation and National Bank shares Inc. between 2007 and 2017. The model was evaluated with the results shows a MAPE for all symbols with less than 3%. A stock prediction method is proposed in in [8] to predict stock price using Elman neural network (ENN). The study optimized the parameter of the model using Grey Wolf optimization (GWO) algorithm.

Model evaluation is testing out on NYSE and NASDAQ data. The results show the proposed model provides high accurate predictions. Ingle and Deshmukh [9] propose a framework for stock market data prediction. The framework use GLM, GBM, Deep learning with PCA, PCR, k- Means models. The model use data of Bombay Stock Exchange to achieve an accuracy of approximately 85%.

Huynh et al. [10] introduce a model that applies LSTM and GRU models to predict and classify stock price movements. The experiment use Reuters and Bloomberg financial news combined with Yahoo Finance price data to forecasting (S&P500) index. Wu et al. [11] propose an integrated prediction method using bi-directional LSTM. The work considers the financial news corpus and the stock technical factors. The work used the dataset from Chinese market and news data for approximately four years. The proposed method achieves superior performance with low overfitting when compared with other baselines methods. Nikou et al. [12] used ANN, SVR, RF, and LSTM data mining techniques to predict close price. The dataset used in the work include the close price of iShares MSCI United Kingdom exchange-traded fund. The results indicates that that the LSTM method functions better in predicting the close price better than the other methods. Pang et al. [13] use LSTM-based prediction method with embedded layer (ELSTM) and based on automatic encoder (AELSTM). Stock historical data used in the implementation includes stock data of the Shanghai A-share market and Shenzhen stock market. Nabipour et al. [14] employed LSTM to predict stock market of Iran. The work use dataset of Petroleum, Non-metallic minerals, Diversified Financials and Basic metals stock market groups. The result shows more accuracy when compared with other learning methods. In [15], Long Short-term memory methods is used with Auto Regressive Integrated Moving Average (ARIMA). Daily EUR/USD exchange rates is used for implementation. The LSTM method produced a better prediction result compared to the ARIMA.

Vargas et al. [16] presented a hybrid Recurrent Neural Networks (RNN) and Convolutional Neural Networks (CNN) technique for stock price movement prediction. Financial news title with technical indicators are used to predicts intraday directional movements using the Standard & Poor's 500 (S&P500) dataset. The implementation result shows some improvement compared with other works. In [17], Long Short-term Memory (LSTM) and Convolutional Neural Network (CNN) is used to predict stock price. The datasets used in the work include S&P500 and Dow Jones (DJIA). The proposed model achieves more accurate predictions than other traditional models. Chavan et al. [1] propose a CNN for predicting the stock price. The data consists of one year stock price of Apple company. Yang et al. [18] present a prediction technique by combining a CNN and LSTM network. The models are applied on S&P 500, DJIA, NASDAQ, NYSE, and RUSSELL stock indices.

3. Methodology

The methodology of the proposed technique makes use of the multivariate time series and LSTM model designs as described in the subsequent subsections.

3.1. Multivariate time series

This study obtains a multivariate time series from the stock historical dataset with a combination of more than one time-dependent variable. Let $x_1(t), x_2(t), \dots, x_K(t)$ represent a set K independent variables with of the variable vector padded to a uniform length of N as shown in Equation 1.

$$x(t) = [x_1, x_2, \dots, x_N] \quad (1)$$

where $x_i(t) \in \mathbb{R}^N$ represent data point with n-dimensions at time t . The independent variable set is drawn from the same underline distribution over M datapoints to form a stack of $K \times M$ multivariate time series X as given in Equation 2.

$$X = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1K} \\ x_{21} & x_{22} & \dots & x_{2K} \\ \dots & \dots & \dots & \dots \\ x_{M1} & x_{M1} & \dots & x_{MK} \end{bmatrix} \quad (2)$$

Let vector $y \in \mathbb{R}^M$ representing M dependent variable vectors drawn from the same distribution as $x_i(t)$. The sequence of the label is also defined in Equation 3.

$$Y = \begin{bmatrix} y_1 \\ y_2 \\ \dots \\ y_M \end{bmatrix} \quad (3)$$

3.2. The LSTM neural network

The proposed LSTM model takes the time sequences x_i as input and yield a predicted values y as output as shown in the structure shown in Figure 1.

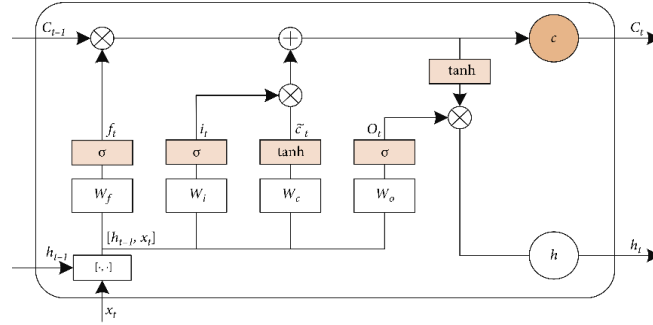


Figure 1. LSTM architecture.

The LSTM model calculates the predicted values using the input, forget, output and with cell candidate gates defined in Equation 4, Equation 5, Equation 6 and Equation 7 respectively:

$$i_t = \sigma_g(W_i x_t + Q_i h_{t-1} + b_i) \quad (4)$$

$$f_t = \sigma_g(W_f x_t + Q_f h_{t-1} + b_f) \quad (5)$$

$$C_t = \sigma_c(W_c x_t + Q_c h_{t-1} + b_c) \quad (6)$$

$$o_t = \sigma_t(W_o x_t + Q_o h_{t-1} + b_o) \quad (7)$$

where i_t represent input gates, o_t represent the output gate, f_t is the forget gate, C_t is the cell candidate, σ_g is the gate activation function, W represent the input weight. R represent the recurrent weight matrices. x_t represent the input vector, and h_{t-1} is the input at the previous time ($t - 1$). b represent the bias vector. The forget gate chooses the prior information to be remembered or forgotten. The cell learns new information, at the input gate, from the input while the output gate passes the updated information from

one timestamp to the next. The cell state C_t and the output h_t at time t are determined as shown in Equation 8 and Equation 9 respectively:

$$c_t = f_t * c_{t-1} + i_t * g_t \quad (8)$$

$$h_t = o_t * \sigma_c(c_t) \quad (9)$$

where $*$ denotes the Hadamard product (element-wise multiplication of vectors).

3.3. Data description and preprocessing

The study employed historical dataset of First Bank of Nigeria Holdings (FBNH) stock in Nigerian Stock market Index from January, 2014 to March 2022. The dataset is obtained online from Capital Asset Ltd, a stockbroking firm with the Nigerian Stock Exchange (NSE), with the URL: www.capitalassetsng.com. The dataset is made up of 1,977 rows and 9 columns. The rows are daily stock transactions listed under the columns: prev close, open, high, low, close, trades, volume, value and date. Features defined from the fields are used to predict the closing price of the next trading day as output. The closing price of the stock between 2014 and 2022 is shown in Figure 2.

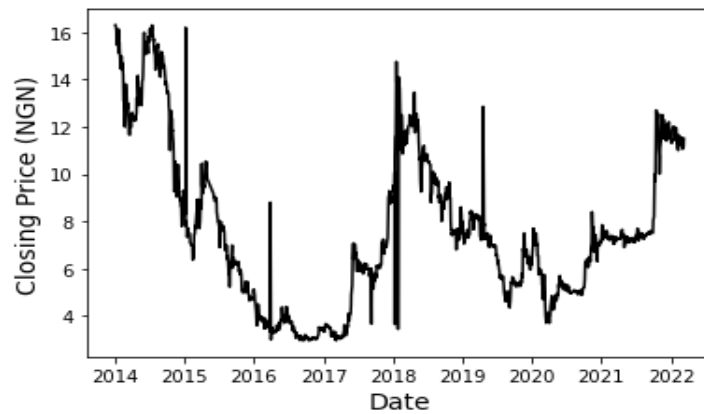


Figure 2. Closing price of the FBNH stock.

The features is defined using previous close, open, high, low, trades, volume and value. The target is defined as the closing price. During the preprocessing the data is normalized and rescaled within a fixed range $[0,1]$ to avoid features with larger value from unjustly interfering and biasing the model and to achieve rapid convergence. The data is also resized to 2D matrix to make it better suited for the deep network training.

3.4. Train, test and validation sets

The dataset is split into train, test and validation sets. The ratio of the train to test split is 90:10 while the train to validation ratio is 80:20. The training set is used to train and make the model learn the hidden patterns in the data. Both the input and output of the training set is used to fit the model. The validation set is used to evaluate the model by fine-tuning the model hyperparameters such as the number of hidden units. Exactly 20 percent of the train data is the validation. The evaluation of the proposed model is carried out using test data after fitting the model using the train and validation sets. In the testing stage, the input element of the testing dataset is provided to the model and predictions are make and compared to the expected values.

4. Results and discussion

4.1. Performance measures

The accuracy of the prediction is measured using metric that includes the mean absolute percentage error (MAPE), mean absolute error (MAE) and root mean square error (RMSE). The execution time for the implementation is also obtained. Mean absolute percentage error is calculated by taking the difference between the actual value and the predicted value and dividing it by the actual value. An absolute percentage is applied to this value and it is averaged across the dataset. The smaller the MAPE, the better the model performance as shown in Equation 10.

$$MAPE = \frac{1}{n} \sum_{i=1}^n \left| \frac{y_i - y'_i}{y_i} \right| \times 100 \quad (10)$$

Where n is the sample size, y_i is the actual data value and y'_i is the predicted data value. The average magnitude of errors of the prediction is gives the mean absolute error measures. The lower the MAE, the higher the accuracy of a model. Mathematically, MAE can be expressed as shown in Equation 11.

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - y'_i| \quad (11)$$

Where y_i is the observed value for the i^{th} observation, y'_i is the predicted value for the i^{th} observation and n is the total number of observations. Mean Squared Error (MSE) measures the the average squared difference between the target variable and the predicted value (see Equation 12):

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - y'_i)^2 \quad (12)$$

Where n is the sample size, y_i is the actual data value and y'_i is the predicted data value. Relative Root Mean Square Error (RRMSE) is the root mean squared error normalized by the root mean square value where each residual is scaled against the actual value as defined in Equation 13:

$$RMSE = \sqrt{\frac{\frac{1}{n} \sum_{i=1}^n (y_i - y'_i)^2}{\sum_{i=1}^n (y'_i)^2}} \quad (13)$$

4.2. Hyperparameter optimization

The proposed model requires certain model parameters to train optimally. These parameters include number of layers, dimension of the input variable and activation function. The initial values of these parameter are as shown in Table 1. Extensive experiments are carried out to find the optimal parameter values for the model.

Table 1. Initial parameters.

Parameter	Value
Activation function	ReLU
LSTM units	10
Epochs	20
Batch size	5
Optimization	Adam

The number of the LSTM unit specifies the capability of the network to memorize the information and correlate it with the past information. The result of the variations of the LSTM unit shows an optimum value of 200 units as shown in Table 2.

Table 2. Effect of LSTM units.

LSTM units	MAPE	MAE	RMSE	RRMSE
10	0.0435	0.6295	0.6773	0.0494
50	0.0523	0.7614	0.8370	0.0554
100	0.0545	0.8002	0.8868	0.0585
150	0.0511	0.7523	0.8444	0.0559
200	0.0325	0.4787	0.5598	0.0378

The batch size refers to the number of samples used to train a model before updating the weights and biases. The model was, thus, tested with different batch sizes as shown in Table 3. The optimal value for batch size was obtained with the batch size 10.

Table 3. Effect of batch size.

Batch size	MAPE	MAE	RMSE	RRMSE
5	0.0125	0.1801	0.2241	0.0157
10	0.0115	0.1606	0.2083	0.0145
20	0.0252	0.3617	0.4272	0.0291
30	0.0588	0.8518	0.9003	0.0668
40	0.5565	7.9473	7.9874	1.2585
50	0.4794	6.8413	6.8723	0.9208

The epoch is used to determine the number of times the training process is repeated using the same training data. Choosing the right value will assist the model to converged and avoid the problem of over-fitting. The optimum result is reached at epoch 150 as shown in Table 4.

Table 4. Effect of epochs.

Epochs	MAPE	MAE	RMSE	RRMSE
10	0.7889	11.2595	11.3088	3.7411
20	0.0209	0.3011	0.3538	0.0251
50	0.0140	0.1961	0.2432	0.0168
100	0.0136	0.1955	0.2416	0.0170
150	0.0119	0.1692	0.2141	0.0150
200	0.0158	0.2295	0.2789	0.0197
250	0.0171	0.2476	0.2994	0.0212
300	0.0155	0.2240	0.2752	0.0194

The activation function ensures the model learns the training dataset well. The results from applying the common activation functions shows that Rectified linear activation function (ReLU) gives the best result as shown in Table 5.

Table 5. Effect of activation function.

Activation function	MAPE	MAE	RMSE	RRMSE
relu	0.0294	0.4240	0.4761	0.0341
sigmoid	0.4824	6.9400	7.0469	0.9612
tanh	0.3486	5.0374	5.1618	0.5589
softmax	0.8641	12.3478	12.4165	6.4573

The optimization algorithms is used to reduce the losses and providing the most accurate results possible. The optimization parameters considered include adagrad, adadelta, SGD, RMSprop and Adam. The results for various optimization techniques are shown in Table 6. From the result is seen that the Adam optimization parameter gives the best performance.

Table 6. Effect of optimization.

Activation function	MAPE	MAE	RMSE	RRMSE
Adadelta	1.0008	14.2815	14.3419	1280.0530
Adagrad	0.9919	14.1563	14.2165	124.1322
Adam	0.0197	0.2821	0.3464	0.0245
RMSprop	0.0272	0.3935	0.4917	0.0334
SGD	0.0632	0.9218	0.9972	0.0653

The implementation of proposed model is carried out using the optimized hyperparameter settings in Table 7. The predicted stock price is obtained for 179 test input data points over a period of 8 months. The predicated values are plotted against the actual outputs as shown in in Figure 3.

Table 7. Optimized hyperparameter settings.

Parameter	Value
Activation function	ReLU
LSTM units	100
Epochs	150
Batch size	10
Optimization	Adam

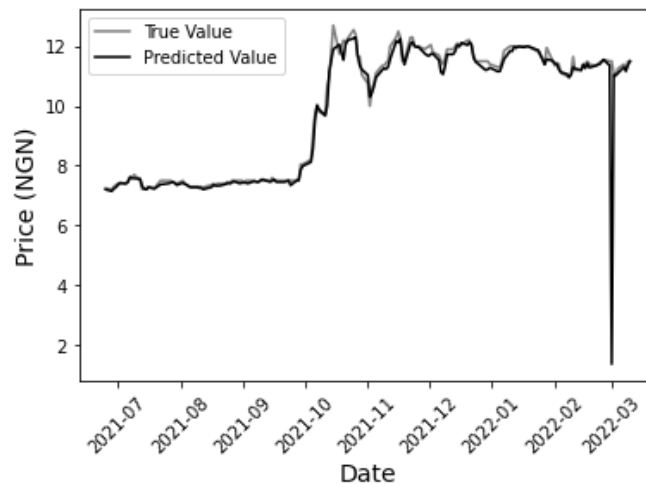


Figure 3. Actual vs predicted stock price.

It is observed that the prediction has lower error and higher accuracies in the first 3 months within the smoother trend in the trading price change. The performance evaluation is also carried out with other machine learning algorithms applied on same dataset. The comparison is as shown in Table 8. The proposed model outperforms the other models on mape, rmse and rrmse performance metric values.

Table 8. Comparison between traditional and proposed techniques.

Prediction Model	MAPE	MAE	MSE	RRMSE
Decision Tree	1.7548	0.0971	0.0971	0.0401
Random Forest	1.6214	0.0893	0.0893	0.0384
SVC	2.2006	0.1359	0.1359	0.0472
KNN	1.8112	0.1146	0.1185	0.0443
AdaBoost	14.8634	0.9010	2.2563	0.1948
Naïve Bayes	2.4466	0.1301	0.1301	0.0461
Gradient Boost	1.4782	0.0893	0.0893	0.0385
RNN	0.2372	0.3943	0.0844	0.0384
Proposed Model	0.0138	0.1255	0.0265	0.0114

5. Conclusion

In this study, a LSTM-based deep learning model is used to predict stock price using multivariate time series. The dataset is obtained from the historical data of First Bank of Nigeria Holdings. The technique creates a multivariate time series from the dataset using previous close, open, high, low, trades, volume and value. The dataset is split into train and test sets for model fitting and evaluation respectively. During the implementation the closing stock price is predicted and the accuracy is measured based on MAPE, MAE, RMSE, rRMSE metrics. The result is compared with other traditional machine learning methods and shows the proposed model performs best on mape, rmse, rrmse.

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