

# ***Dynamics of Salinity and Erosion in Wave-Cut Platforms: Investigating White Cliffs in England Through the Lens of the Boussinesq Approximation***

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**Abstract.** This study investigates coastal erosion at the White Cliffs of England using a wave-cut platform model and in situ  $^{10}\text{Be}$  exposure testing. By integrating a salt conservation model within the Boussinesq approximation, the research aims to quantify salinity evolution in the English Channel and assess its contribution to chalk cliff instability. Results indicate that salinity-driven crystal growth reduces rock integrity by up to 55%, with pronounced seasonal variation in erosion rates, particularly during late winter. This interdisciplinary approach offers insight into the coupling between fluid mechanics, sediment dynamics, and climate-driven coastal change.

**Keywords:** abrasion, Boussinesq approximation, chalk cliffs, coastal erosion, salinity, wave-cut platforms

## **1. Introduction**

White cliffs, formed by micro-organisms in the sea, have been an iconic landscape along the south coast of England since the Cretaceous Period. They are mainly made of limestone and are erosion-prone by seawater in the English Channel. A study finds that England contributes 30% of the erosion that damages 17% of the UK coastline [1]. Therefore, there is a requirement for a dynamic model of cliff erosion to show coastal processes.

The wave-cut platform model involves various physical and geological processes. Its unique traits are shaped by complex coastal erosion, abrasion, and hydraulic action. In hydraulic action, the waves crash against the cliffs and push air into the cracks with enormous pressure, especially during storms. This compressed air pushes out parts of the cliff face. During abrasion, pebbles grind along the rock platforms and form a north face shaped by the waves. The lack of foundation leads to the collapse and retreat of the cliff.

Waves transport water and sediment and cause the physical erosion of rock surfaces. The speed of erosion depends on factors such as wave energy, height, period, and material type. The Shoreline Erosion Index expresses the relationship between wave strength, energy per unit time, and erosion, taking into account wave height, period, and other parameters.

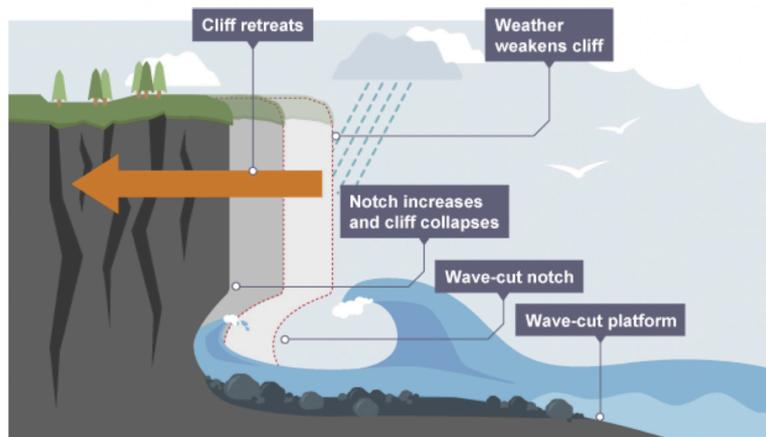


Figure 1: Coastal processes image, called erosion, mass movement and weathering break down and remove material from the coast. The material is moved along the coastline by the sea and deposited when there is energy loss [2]

## 2. Materials and methods

### 2.1. Testing the erosion rate with $^{10}\text{Be}$

The first stage in creating predictive models for future coastal change is figuring out how quickly coasts have eroded in the past and what causes coastal change.  $^{10}\text{Be}$  is the formation of an exposed rocky platform when the cliff recedes. Analysing in situ  $^{10}\text{Be}$  concentrations on rocky coasts helped researchers predict cliff retreat rates and understand Quaternary exposure, inheritance, and reoccupation of coastal platforms [3]. The model (Figure 2) suggests that coastline profile changes due to equilibrium retreat, with cliff height, platform gradient, and beach width remaining constant [4]. Research in East Sussex, UK, shows that soft chalk cliffs have eroded at rates ranging from  $2\text{--}6\text{ cm}\cdot\text{yr}^{-1}$  over 7,000 years to  $10\text{--}80\text{ cm}\cdot\text{yr}^{-1}$  over 150 years [5], indicating a need for investigation into the cause.

Meanwhile, researchers have discovered that coastal cliffs are collapsing due to the formation of salt crystals in chalk samples. The strength of coastline samples was 20–55% lower than quarry samples [6], indicating salt as the main cause of the weakness. These crystals, created when saltwater evaporates, distort the rock's shape, weakening the structure and causing the cliff to collapse. The study also raises questions about how salinity accelerates erosion.

### 2.2. Salt crystallisation: Conservation model in the boussinesq equation

Salt stresses and strains rocks in three main ways: volume change due to hydration, temperature-induced salt crystal expansion, and crystal formation from solution. Salt crystals can expand due to water absorption and thus create stresses in the rock. The salt concentration in the capillaries of the rock can lead to decomposition in places with strong diurnal fluctuations. Coastal cliffs absorb a lot of salt from bubbles and sea spray [7].

The salt conservation model considers the salinity distribution in water bodies over time and space. The change in the amount of salt is equal to the sum of the salt fluxes due to currents

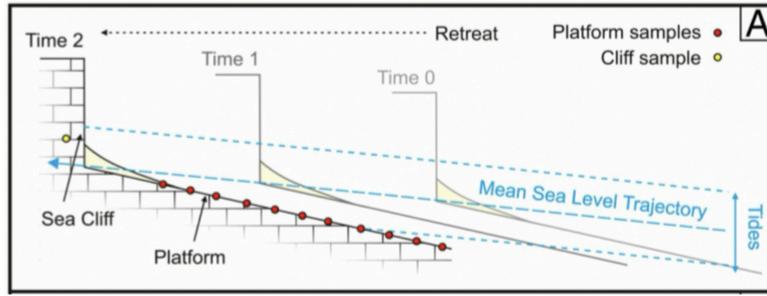


Figure 2: Setup for modelling the accumulation of  $^{10}\text{Be}$  on a coastal platform. The model assumes equilibrium retreat such that as the coast evolves the cross-section morphology remains steady while translating shoreward according to the prescribed retreat rate. Beach width was held constant during each model run, and the elevation of the coastal profile tracks relative sea level change [4]

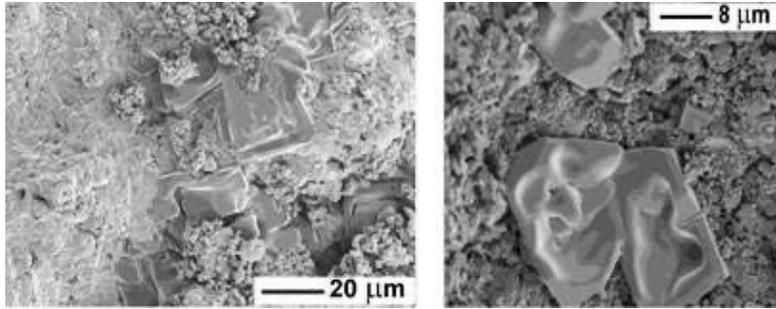


Figure 3: Chalk matrix under the microscope. Zoom out at a scale of  $20\mu\text{m}$  and zoom in at a scale of  $8\mu\text{m}$  [6]

and diffusion, which result from the conservation of mass and diffusion processes, by using the following formula:

$$\frac{\partial(\rho S)}{\partial t} + \nabla \cdot (\rho \mathbf{u} S) = \nabla \cdot (\rho D \nabla S) \quad (1)$$

This full form accounts for variable density  $\rho$  and spatially varying salinity  $S$ .

Under the Boussinesq approximation, where density variations are assumed negligible, this simplifies to [8]:

$$\frac{\partial S}{\partial t} + \mathbf{u} \cdot \nabla S = D \nabla^2 S \quad (2)$$

This is a mathematical framework used to describe the temporal and spatial variations of salinity (or solute concentration) in water bodies. In this equation,  $S$  stands for salinity, which varies both temporally and spatially, whereas  $t$  stands for time. The fluid velocity vector  $\mathbf{u}$  describes the water movement, and  $\nabla$  stands for the gradient operator, which expresses spatial gradients.  $D$ , the diffusion coefficient, characterises the diffusion of salinity due to differences in concentration. The left-hand side describes the development of salinity over time, while the right-hand side reveals the contributing factors. The first term,  $\mathbf{u} \cdot \nabla S$ , accounts for convective effects caused by fluid movement and represents spatial transport. The second term,  $D \nabla^2 S$ , shows how salinity moves

through space because of differences in concentration. It does this by using the Laplacian operator ( $\nabla^2$ ), which represents spatial diffusion.

This equation is applicable for characterising the changes in saltwater concentration in the English Channel, especially when both the fluid movement and the diffusion processes induced by the concentration gradients play a significant role. The solution of this equation facilitates the simulation of the dynamic evolution of salinity in the channel and provides an understanding of how different factors affect the distribution of salinity. Notably, particular simulations necessitate suitable initial conditions, boundary conditions, and parameter values; furthermore, the resolution may require the use of numerical methods.

### 3. Results

#### 3.1. Salt weathering in different seasons causes different erosion rate

In line with the previously discussed equations and additional data, the English Channel shows remarkable regional differences in late winter (February). The western region has higher surface salinity (35.3) and higher temperatures (9–10°C), while the eastern side has lower salinity (35.0) and cooler temperatures (6–6.5°C), a correlation consistent with observed seasonal patterns. In summer (August), there is a slight decrease in salinity (0.1–0.3) with a simultaneous increase in temperature (15–17°C), which corresponds to the expected climatic changes. East of 2°W, tidal mixing provides a uniform temperature and salinity, while west of 3°W, a distinct thermocline is evident, limiting summer bottom temperatures to 10–11°C [9]. In addition, the tidal waves penetrate from the Atlantic to the English Channel. The tidal range is greater on the south side of the strait due to the Earth's rotation and the topography. Famous places are Saint-Marie on the French coast, Lobay and the Somme estuary. At spring tide, the tidal range can be up to 13.5 metres, and the tidal velocity in the Alderney Waterway is 5.0 metres per second [9].

During frost and salt crystallisation weathering, moisture is absorbed in the rock, which leads to decomposition and stresses. This can hydrate minerals, which leads to expansion and contraction and thus to cracks. These observations emphasise the seasonal dynamics and regional influences that characterise the hydrodynamics of the English Channel. It can be concluded that there is a risk of large collapses during extreme weather conditions, especially from February to March.

#### 3.2. Limitations vs. improvements of the boussinesq approximation

The Boussinesq approximation, a useful tool to describe fluid dynamics, has its limitations due to the assumption of constant fluid density. This affects accuracy in scenarios with significant temperature or salinity gradients and is unsuitable for turbulent or unsteady flows. It is also only partially suitable for simulating shallow water waves and coastal conditions.

To overcome these limitations, researchers can use advanced fluid dynamics models to accurately capture density effects on fluid motion. The salt conservation model under the Boussinesq approximation requires a sophisticated approach, including Navier–Stokes equation, transport equations, and seawater mixing models. Validation methods can improve accuracy. This interdisciplinary approach, combining fluid dynamics, thermodynamics, and oceanographic principles, promises a refined understanding of dynamic salinity patterns in the English Channel.

## 4. Implications

### 4.1. Climate and sea level changes

White cliffs are usually made of limestone, rich in calcium carbonate ( $\text{CaCO}_3$ ), making them susceptible to erosion. Limestone eroded by acid in the sea can lead to the release of  $\text{CO}_2$  and help reduce ocean acidity. The following chemical reaction is:



The increasing frequency of storms can also accelerate the erosion of limestone and influence carbon dynamics. This causes climate change and sea level changes directly.

### 4.2. Rock resistance and sediment transport

By calculating the erosion rate of the wave-cut platform, varied rock resistances can be determined. The link between rock properties and erosion rates, which includes salt-induced abrasion, may also be described numerically.

Sediment transport by waves, influenced by salt, significantly affects erosion and deposition processes on wave-cut platforms. During strong waves, sediments form a sandbar, transferring sand away from the beach and depositing it in deeper areas. As wave energy decreases, sediments on the sandbar are gradually pushed back onshore. This sediment movement process is crucial in shaping coastal landscapes, redistributing sand, and maintaining the dynamic equilibrium of the beach environment.

## 5. Conclusion

The study of erosion dynamics on rocky coasts with limestone formations reveals a complex interplay of geological, climatic, and anthropogenic factors. Limestone's susceptibility to erosion, exacerbated by climate change, has potential  $\text{CO}_2$  implications. The wave-cut platform model emphasises hydraulic action, abrasion, and lack of foundations. The  $^{10}\text{Be}$  test method and salt preservation model under the Boussinesq approximation provide insights into historical erosion rates and salt's influence on coastal stability. Understanding and mitigating coastal risks is crucial for climate change, sea level change, rock resilience, and sediment transport. Protective measures, such as vegetative cover, structural support, and beach nourishment, are essential. Future research can focus on refining models for complex meteorological and tidal conditions and investigating human impacts on coastal stability.

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