U.S. unemployment rate prediction using time series model

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Abstract. Although previous studies have given a better prediction model for the American's unemployment rate, due to the short time and different time nodes, the parameters of the model and the seasonality and the stability of the time series are also different. In this study, the ARIMA model, which is the most widely used in the time series, is adopted and the seasonal influence is added to the model according to the selected time period. At the same time, two models are used to predict the unemployment rate in the United States from January 2017 to January 2019. The stability of the model was determined by Dickey-Fuller test, and the fitting and prediction effects of the two models were compared by comparing the values of AIC and MSE. With the fitting prediction method of the unemployment rate in the United States, this paper can analyze and predict the unemployment rate in other Western countries, and can further compare and analyze the reasons with China 's unemployment rate, which is convenient for us to better regulate macroeconomic policies.

Keywords: Unemployment rate, time series analysis, ARIMA, SARIMA, unit root test.

1. Introduction

Unemployment rate is an important economic indicator reflecting the utilization of labour resources in a country or region, and it is the main goal of adjusting macroeconomic policies in various countries. Generally speaking, the rising unemployment rate means that more labor force cannot be fully utilized. With the increase of unemployment, the total demand of society will gradually decline, and the driving force of economic growth will be weakened. Therefore, governments use the unemployment rate as an important basis for judging the degree of economic health when adjusting domestic economic and monetary policies and supply and demand relations [1].

Time series analysis is a statistical method used to analyze and predict time series data [2]. Its goal is to understand the patterns, trends and periodicity in the data, and to predict and make decisions accordingly. The researches have a wide range of applications in many fields, including medicine [3, 4], economics [5], finance [6], meteorology [7]. According to the monthly data of the U.S. unemployment rate (USUR) from the U.S. Bureau of Labor Statistics [8], the proportion of total employment in the United States is gradually increasing, but the unemployment rate fluctuates greatly. Among them, the period in which the unemployment rate in the United States grew more rapidly is roughly 1975-1977, 1980-1986 and 2008-2009, which correspond to the United States inflation, the oil crisis and the global financial crisis. The research of Xue [9] and Shao [10] shown that the monthly data of unemployment

rate in the United States can be analyzed by time series analysis method to fit the model and predict the unemployment rate in the future.

By observing the monthly data of the unemployment rate in the America since January 1948, researches established an ARIMA model for USUR for fitting, analysis and prediction [11]. The lack of literature can be attributed to the following points: Take the industrial structure, national macroeconomic regulation and monetary policy as the starting point for analysis and research. Most of the domestic data are used as research samples, and there is no comparative analysis of other countries. The object of analysis is limited to the urban or overall unemployment rate, and there is a lack of analysis of the employment of young people [12]. The establishment of the model only uses the unemployment rate of the United States, and analyzes it against the background of the US market economic system. There is no expansion of the scope to establish a more universal time series prediction model, and there is a lack of a control group under similar economic systems.

In this paper, the influence of the stability and seasonality of time series on the model is considered when establishing the model. In order to increase the stationarity of the data to correctly establish the model, logarithmic preprocessing, residual white noise test and differential unit root test are used. Considering the influence of seasonality, after consulting the data, we choose to add seasonal factors to the original ARIMA model. After comprehensive consideration and comparison, we choose a more appropriate prediction model to predict the unemployment rate of the United States in the next 24 periods.

2. Methods

2.1. Data source

The U.S. data used in this paper is derived from the official database of Labor Statistics, and selects the monthly unemployment rate data of the United States from January 1948 to January 2019. Firstly, the time series diagram of the data is drawn, such as Figure 1.

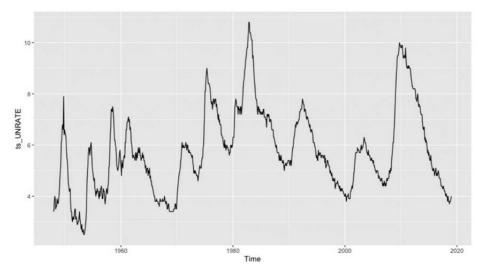


Figure 1. Unemployment Rate of China and US.

In Figure 1, we can find that the unemployment rate in the U.S. is up to its lowest in 1954 and reached its highest in 1984. From 2008 to 2009, due to the impact of the global economic crisis, the U.S. unemployment rate grew rapidly. It can be seen from the time series diagram that the fluctuation of unemployment rate in the United States is regular, so the unemployment rate in the U.S. may have seasonal factors.

In addition, seeing the large time span of the selected data and the large fluctuation of the unemployment rate data, the logarithm of the time series data is stable.

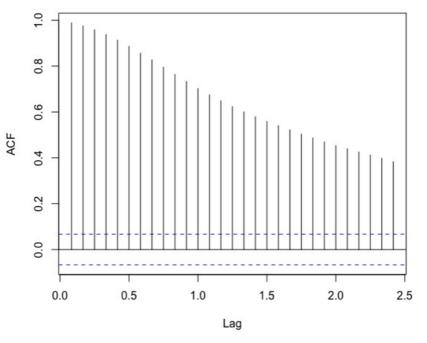
2.2. Model selection

The main purpose of analysis of time series is to predict future nodes based on the data corresponding to historical time. The commonly used prediction models are AR model, MA model, ARMA model, ARIMA model and SARIMA model. Among them, the ARIMA model has been applied by many scholars in different fields to analyze and predict time series. According to the time series image of the selected data, it is speculated that the selected data may be seasonal. This paper will use ARIMA to analyze the time series of the unemployment rate in the United States, and add seasonal factors to the model. This paper selects the unemployment rate from January 1948 to December 2016 as the sample set to determine the parameters of the model for fitting, and then uses the unemployment rate data from January 2017 to January 2019 as the test set to substitute into the model for prediction.

3. Results and discussion

3.1. ARIMA model

The standard form of ARIMA model is ARIMA(p, d, q), where AR and MA represent autoregressive process and moving average process respectively. The parameters p and q are the autocorrelation order and the moving average order. Parameter d represents the difference order required to convert a non-stationary sequence into a stationary time series. In the data preprocessing part, in order to make the unemployment rate more stable, the logarithm is taken. However, according to the autocorrelation test, as shown in Figure 2, we find that the autocorrelation is strong and the ACF function continues to tail, so the time series data is still non-stationary.



Autocorrelations of the US

Figure 2. Autocorrelations of the US.

The time series data after logarithm is still not stable, so in order to make the time series more stable and facilitate the establishment of the model, we perform first-order difference and second-order difference on the training sample data after logarithm. According to the improved unit root test (ADF test) based on the Dickey-Fuller test, the p values of the first-order difference and the second-order difference are both less than 0.01, so the null hypothesis (the time series is unstable) is rejected on the basis of the 99 % confidence interval, that is, the first-order difference and the second-order difference are both stationary time series. As hinted in Table 1.

	Dickey-Fuller	Lag order	P-value
First-order-difference	-8.2816	9	0.017
Second-order-difference	-12.666	9	0.012

 Table 1. ADF test of the first-order-difference and the second-order-difference.

It can be told from Figure 3 and Figure 4 that the 2nd-difference is more stable than the first harmonic coil order difference. In terms of volatility, the fluctuation degree of the 1st-difference is greater than that of the second-order difference. The data after the first difference is between 0 and 0.05, while that after the second difference is between 0 and 0.03. Therefore, the parameter d is 2. Therefore, the model can be set to ARIMA (p, 2, q). Next, we do the ACF graph (Figure 5) and the PACF graph (Figure 6) of the second difference. From the graph, we can see that the autocorrelation function is second-order truncated, so q can be taken as 0,1,2, and the partial autocorrelation coefficient is fourth-order truncated, so 0,1,2,3,4 can be taken.

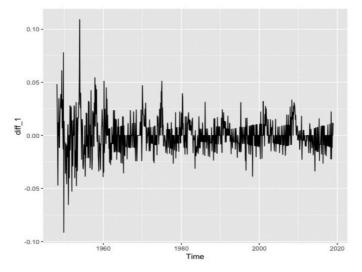


Figure 3. Autocorrelations of the US.

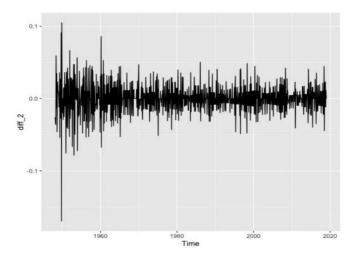
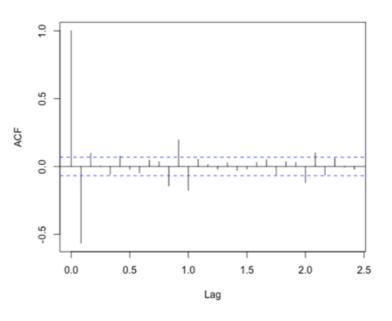
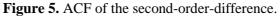
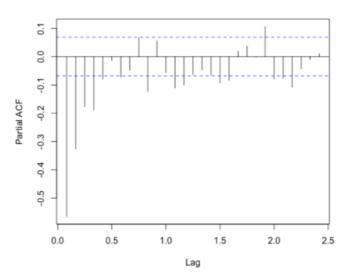


Figure 4. The second-order-difference.



ACF of the second-order-difference





PACF of the second-order-difference

Figure 6. PACF of the second-order-difference.

From the above analysis, 15 possible ARIMA models can be obtained. In order to select the most suitable parameter values, the MSE, AIC and BIC of different parameter values in the ARIMA model are compared. The training set is used to test the regression prediction results of 15 models. The lower values of MSE, AIC and BIC are, the more suitable the fitting degree of the model is. Table 2 shows the results of the 15 models.

ARIMA(p,2,q)	MSE	AIC	BIC
ARIMA(0,2,0)	0.0786	246.633	256.064
ARIMA(0,2,1)	0.0427	-254.843	-240.697
ARIMA(0,2,2)	0.0417	-272.783	-253.922
ARIMA(0,2,3)	0.0416	-273.294	-249.718
ARIMA(0,2,4)	0.0416	-271.941	-243.649
ARIMA(1,2,0)	0.0507	-112.326	-98.180
ARIMA(1,2,1)	0.0416	-274.602	-255.740
ARIMA(1,2,2)	0.0416	-272.671	-249.095
ARIMA(1,2,3)	0.0415	-271.881	-243.588
ARIMA(1,2,4)	0.0413	-274.426	-241.418
ARIMA(2,2,0)	0.0450	-209.241	-190.379
ARIMA(2,2,1)	0.0416	-272.710	-249.133
ARIMA(2,2,2)	0.0416	-270.603	-242.310
ARIMA(2,2,3)	0.0412	-276.851	-243.843
ARIMA(2,2,4)	0.0409	-280.925	-243.202

 Table 2. ARIMA model results

From Table 2, it is found that the minimal values of MSE, AIC and BIC are appeared in the model of ARIMA (2,2,4), which is the best fit among all 15 models. Combining the predicted value of ARIMA (2,2,4) with the actual image of the training set, as shown in Figure 7. It can be found that the fitting effect of the predicted value of the model fitting and the original real data is not good, indicating that seasonality has a great influence on the fitting prediction effect of the ARIMA model.

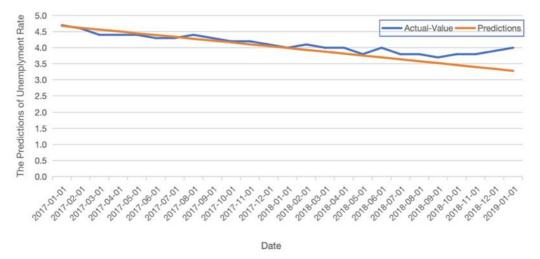


Figure 7. Plot of the predict value.

3.2. SARIMA model results

SARIMA is seasonal ARIMA, which can be expressed as SARIMA (p, d, q) \times (P, D, Q) [S]. The first half represents the non-seasonal part, and the second half denotes by the seasonal part, where S

represents the seasonal frequency. The auto.arima function can be used to automatically determine the order in R, and the AICc criterion is the default criterion. The results are shown in Table 3.

α_{I}	α_2	α_3	Ma1	Sar1	Sar2	Sma1	Sma2	σ^2
0.5099	0.2131	0.0771	-0.5171	0.5786	-0.1373	-0.8295	0.0818	0.03597

Table 3. Coefficients of the ARIMA(3,1,1)(2,0,2)[12]

From the running results, it can be concluded that the model SARIMA(3,1,1) \times (2,0,2)[12] fits best as to the value of AIC=-384.13,AICc=-383.9 and BIC = -341.79. Therefore, we use the results of this model to fit the training set and predict the time series of the test set. The fitting error RMSE = 0.1886159 < 0.5 of the training set can be obtained (table 4).

Table 4. Results of error measures							
	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	0.00251	0.1886	0.1387	0.01934	2.547	0.1562	-0.00172

The model's residuals are calculated and the Box-Ljung Test is used to determine whether the residuals are significant, so as to test whether the residuals are white noise sequences. The running results are shown in Table 5, p-value = 0.9606 > 0.05, indicating that the residual sequence accepts the null hypothesis under the 95 % confidence interval and is already white noise. There is no autocorrelation in the time series data, and the model fully extracts the effective information in the data (Figure 8).

Table 5.	The	results	of	Box-I	Ljung	test
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	X-squared	Difference	P-value
Residuals	0.002443	1	0.9606

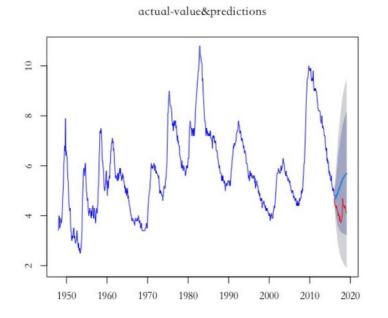


Figure 8. Prediction and actual values' comparison.

4. Conclusion

In this paper, ARIMA(2,2,4)and SARIMA(3,1,1)×(2,0,2)[12]are used to fit the time series of the US unemployment rate. In the fitting process, this paper finds that the RMSE of ARIMA(2,2,4)is 0.2023, while the RMSE of SARIMA(3,1,1)×(2,0,2)[12] is 0.1886159, which is slightly lower than that of ARIMA(2,2,4). Therefore, the optimal model for fitting the time series data of USUR from January 1948 to December 2016 is SARIMA(3,1,1)×(2,0,2)[12], so SARIMA(3,1,1)×(2,0,2)[12] can better predict the change of USUR from January 2017 to January 2019. However, from the experimental results of this paper, the final prediction effect of the two models is not very good, and there may be other macro variables that this paper ignores that have a certain impact on the change of time series data. In the future, more in-depth exploration can be carried out to find other influencing factors and more optimized fitting prediction schemes.

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